

Вариант 1

$$1. \int \left(1 - \frac{1}{x^2}\right) \sqrt{x\sqrt{x}} dx$$

$$2. \int \frac{dx}{2^x + 4 \cdot 2^{-x}}$$

$$3. \int \frac{(5x + 1) dx}{x^2 - 8x + 25}$$

$$4. \int x \cdot \operatorname{arctg}(2x) dx$$

$$5. \int \frac{x^3 + 2}{x^3 - 8x^2 + 7x} dx$$

$$6. \int \frac{x^3}{(x - 2)^2(x^2 + 2x + 10)} dx$$

$$7. \int \operatorname{tg}^6 2x dx$$

$$8. \int \frac{\sin^2 x}{\sin x + 2\cos x} dx$$

$$9. \int \frac{dx}{\sqrt[3]{x} + 8}$$

$$10. \int \frac{dx}{(x^2 + 3)\sqrt{4 - x^2}}$$

Вариант 2.

1. $\int \frac{2^{x+1} - 5^{x+1}}{10^x} dx$

2. $\int \frac{dx}{x \ln x \sqrt{\ln \ln x}}$

3. $\int \frac{(3x - 1) dx}{\sqrt{9 + 8x - x^2}}$

4. $\int \arccos(5x) dx$

5. $\int \frac{x^4}{x^3 + 8x^2 + 7x} dx$

6. $\int \frac{x^3 + 1}{(x^5 + 2x^3 + 10x^2)} dx$

7. $\int \frac{dx}{\sin^3 x \cos^5 x}$

8. $\int \frac{dx}{\sin^4 x + \cos^4 x}$

9. $\int \frac{dx}{(1 + \sqrt[4]{x})\sqrt{x}}$

10. $\int \frac{dx}{(x^2 + 1)(x + \sqrt{x^2 + 1})}$

Вариант 3.

$$1. \int \frac{\sqrt{x^2 + 1} + \sqrt{x^2 - 1}}{\sqrt{x^4 - 1}} dx$$

$$2. \int \operatorname{tg} \frac{1}{x} \cdot \frac{dx}{x^2}$$

$$3. \int \frac{(7x - 2)dx}{\sqrt{11 - 10x - x^2}}$$

$$4. \int \ln(x^2 + 3) dx$$

$$5. \int \frac{x^3 - 2}{x^3 + 8x^2 + 7x} dx$$

$$6. \int \frac{x^3 + 1}{(x - 3)^2(x^4 + 2x^2)} dx$$

$$7. \int \frac{dx}{\sin^4 x \cos^2 x}$$

$$8. \int \frac{\cos^2 x dx}{(\sin^2 x - 4\cos^2 x)^2}$$

$$9. \int \frac{1 - \sqrt{x + 1}}{1 + \sqrt[3]{x + 1}} dx$$

$$10. \int \frac{\sqrt{x^2 - 1}}{x} dx$$

Вариант 4.

$$1. \int \frac{\sqrt{1+x^2} + \sqrt{1-x^2}}{\sqrt{1-x^4}} dx$$

$$2. \int \frac{dx}{\sin^2 x \sqrt[3]{\operatorname{ctg} x}}$$

$$3. \int \frac{(7x+3)dx}{x^2 - 10x + 29}$$

$$4. \int \frac{\sin x}{e^x} dx$$

$$5. \int \frac{x^4}{x^3 - 8x^2 + 7x} dx$$

$$6. \int \frac{x}{(x+2)^2(x^2 - 2x + 10)} dx$$

$$7. \int \frac{dx}{\cos^4 2x}$$

$$8. \int \frac{dx}{(3\sin 2x + 2\cos 2x)^2}$$

$$9. \int \frac{x dx}{\sqrt[3]{2x-3}}$$

$$10. \int \frac{x^3}{\sqrt{9-x^2}} dx$$

Вариант 5.

1. $\int \frac{e^{3x} - 1}{e^x - 1} dx$

2. $\int \frac{\operatorname{ctg} \sqrt{x}}{\sqrt{x}} dx$

3. $\int \frac{(9x - 2)dx}{\sqrt{x^2 + 10x + 9}}$

4. $\int \frac{\ln x}{\sqrt{x}} dx$

5. $\int \frac{x^4}{x^4 + 5x^2 + 4} dx$

6. $\int \frac{x + 1}{(x^5 - 2x^3 + 50x^2)} dx$

7. $\int \cos^2 2x \cdot \cos^2 5x dx$

8. $\int \frac{\sin x \cdot \cos x dx}{\sin x + \cos x}$

9. $\int \frac{dx}{(x+1)^4 \sqrt{x^3}}$

10. $\int \frac{dx}{\sqrt{9x - x^2}}$

Вариант 6.

1. $\int \frac{x-4}{2x+4\sqrt{x}} dx$

2. $\int \frac{2 + 3 \operatorname{ctg}^2 x - \cos x}{\sin^2 x} dx$

3. $\int \frac{(3x + 1)dx}{\sqrt{x^2 + 4x + 3}}$

4. $\int \frac{\ln x}{x^2} dx$

5. $\int \frac{x^4 + 1}{x^4 + 3x^3 - 4x} dx$

6. $\int \frac{x^2 + 8}{(x^2 + 2x + 2)(x - 3)} dx$

7. $\int \sin^2 3x \cdot \sin^2 4x dx$

8. $\int \frac{dx}{\sin^6 x}$

9. $\int \frac{3-\sqrt{x+2}}{x+2\sqrt{x+2}} dx$

10. $\int x^2 \sqrt{4 - x^2} dx$

Вариант 7.

1. $\int (\sqrt{x^7} - \sqrt{7^x}) dx$

2. $\int \frac{5 - x^2 + e^{\sqrt{x}}}{\sqrt{x}} dx$

3. $\int \frac{(2x + 1) dx}{x^2 - 4x + 13}$

4. $\int x \cdot ctg^2 x dx$

5. $\int \frac{x^3 - 1}{x^3 + 2x^2 - 15x} dx$

6. $\int \frac{x - 1}{x^4 + 2x^3 + 5x^2} dx$

7. $\int \frac{\cos^5 x}{\sin^2 x} dx$

8. $\int tg^3 x dx$

9. $\int \frac{3-x}{1+\sqrt[3]{x-2}} dx$

10. $\int x^2 \sqrt{x^2 - 4} dx$

Вариант 8.

1. $\int 2^{2x} \cdot 3^{3x} \cdot 4^{4x} dx$

2. $\int \frac{8x^3 - 2x}{\sqrt{1 - x^4}} dx$

3. $\int \frac{(2x - 4)dx}{\sqrt{x^2 + 4x + 5}}$

4. $\int \operatorname{arctg}(2x) dx$

5. $\int \frac{x^5 + 1}{x^4 - 9x^2} dx$

6. $\int \frac{x^2}{x^3 + 8} dx$

7. $\int \frac{\sin^5 x}{\cos^3 x} dx$

8. $\int \frac{\cos x}{2 + \sin x - 3 \cos x} dx$

9. $\int \frac{\sqrt[3]{x} + 2}{\sqrt{x} + \sqrt[6]{x}} dx$

10. $\int \frac{\sqrt{9 - x^2}}{x^2} dx$

Вариант 9.

1. $\int \frac{\sqrt{x}-8}{\sqrt{x}-2\sqrt[3]{x}} dx$

2. $\int \frac{x^4 + 2 + \sin \ln x}{x} dx$

3. $\int \frac{(5 - 3x)dx}{x^2 + x + 1}$

4. $\int \cos \ln x dx$

5. $\int \frac{x^4}{x^4 - 8x^2 + 16} dx$

6. $\int \frac{1}{(x^2 - 2x + 5)(x^2 + 1)} dx$

7. $\int \frac{\sin^5 x}{\cos^2 x} dx$

8. $\int \operatorname{ctg}^6 x dx$

9. $\int \frac{x-3}{\sqrt{x+1}+3} dx$

10. $\int x^2 \sqrt{x^2 + 4} dx$

Вариант 10.

1. $\int e^x(5 - \frac{e^{-x}}{\sqrt[3]{x}})dx$

2. $\int \frac{5 - \sqrt{\operatorname{arctg} x}}{x^2 + 1} dx$

3. $\int \frac{(2x + 5)dx}{\sqrt{1 - x + x^2}}$

4. $\int \ln^2 x dx$

5. $\int \frac{x^3}{x^3 - 4x^2 + 5x - 2} dx$

6. $\int \frac{x}{x^4 + 5x^2 + 4} dx$

7. $\int \sin^7 x dx$

8. $\int \frac{dx}{\cos^2 x \sin^6 x}$

9. $\int \frac{\sqrt[3]{x}-3}{\sqrt{x}+2\sqrt[3]{x}} dx$

10. $\int \frac{\sqrt{x^2 - 9}}{x^2} dx$

Вариант 11

1. $\int \frac{(1-3x^2)dx}{x^2(1+x^2)}$

2. $\int \frac{dx}{x\sqrt{1-\ln^2 x}}$

3. $\int \frac{(3x-5)dx}{\sqrt{-4x-x^2}}$

4. $\int x^2 \cos x dx$

5. $\int \frac{x^3+2}{x^3-4x} dx$

6. $\int \frac{3x-5}{x^4-4x^3+8x^2} dx$

7. $\int \frac{\cos^8 x dx}{\sin^2 x}$

8. $\int \frac{(8+tgx)dx}{18\sin^2 x+2\cos^2 x}$

9. $\int \sqrt{\frac{6-x}{x-14}} dx$

10. $\int \frac{dx}{\sqrt{(5-x^2)^3}}$

Вариант 12

1. $\int \frac{x^5 + x^2 \cdot 3^x - \sqrt{x}}{x^2} dx$

2. $\int \sqrt{1 + \cos x} \sin x dx$

3. $\int \frac{(x+8) dx}{x^2 - 6x + 13}$

4. $\int x^3 \ln x dx$

5. $\int \frac{(x^3 + x^2 + 1) dx}{x^3 - 5x^2 + 6x} =$

6. $\int \frac{(x^2 + 1) dx}{x^2(x^2 + 4)}$

7. $\int \frac{\sin^2 x}{\cos^8 x} dx$

8. $\int \frac{\cos x dx}{(1 - \cos x)^3}$

9. $\int \sqrt{\frac{9 - 2x}{2x - 21}} dx$

10. $\int \frac{dx}{(9 + x^2)^{\frac{3}{2}}}$

Вариант 13

1. $\int \frac{(2-x)^2 dx}{x(x^2+4)}$

2. $\int \sin^4 x \sin 2x dx$

3. $\int \frac{(5-x) dx}{\sqrt{9+8x-x^2}}$

4. $\int (x^2 - 6x + 5)2^x dx$

5. $\int \frac{x+2}{x^3-9x} dx$

6. $\int \frac{xdx}{(x-1)^2(x^2-2x+2)}$

7. $\int 256 \sin^8 x dx$

8. $\int \frac{3+2\operatorname{tg}x}{2\sin^2 x+3\cos^2 x-1} dx$

9. $\int \frac{x\sqrt{1+x}}{\sqrt{1-x}} dx$

10. $\int \frac{\sqrt{x^2-4}}{x^4} dx$

Вариант 14

1. $\int (2^x + 3^x)^3 dx$

2. $\int \frac{x^5 dx}{1+x^{12}}$

3. $\int \frac{(4x+7) dx}{x^2 - 10x + 50}$

4. $\int e^{3x} \cos 5x dx$

5. $\int \frac{2x^3 - 40x - 8}{x(x+4)(x-2)} dx$

6. $\int \frac{3x^3 + x + 46}{(x-1)^2(x^2+9)} dx$

7. $\int \sin^2 x \cos^6 x dx$

8. $\int \frac{2\operatorname{ctg} x + 1}{(2\sin x + \cos x)^2} dx$

9. $\int \frac{1 - \sqrt[6]{x} + 2\sqrt[3]{x}}{x + 2\sqrt{x^3} + \sqrt[3]{x^4}} dx$

10. $\int x^2 \sqrt{1-x^2} dx$

Вариант 15

1. $\int (\cos^4 \frac{x}{2} + \sin^4 \frac{x}{2}) dx$

2. $\int \frac{e^x dx}{1 + e^{2x}}$

3. $\int \frac{(5x-4) dx}{\sqrt{3+2x-x^2}}$

4. $\int \frac{\ln x dx}{\sqrt[3]{x}}$

5. $\int \frac{x^3 + 1}{x^2 - x} dx$

6. $\int \frac{x^3 + 2x^2 + 10x}{(x+1)^2(x^2 - x + 1)} dx$

7. $\int \sin^2 x \cos^6 x dx$

8. $\int \frac{dx}{\sin^2 x(1 - \cos x)}$

9. $\int \frac{x + \sqrt{3x-2} - 10}{\sqrt{3x-2} + 7} dx$

10. $\int \frac{dx}{\sqrt{(4-x^2)^3}}$

Вариант 16

1. $\int \frac{(1 - 4\operatorname{ctg}^2 x) dx}{\cos^2 x}$

2. $\int \frac{e^{\operatorname{arcsin} x} + x - 1}{\sqrt{1 - x^2}} dx$

3. $\int \frac{3x - 1}{\sqrt{1 - 6x - x^2}} dx$

4. $\int e^{\sqrt{x}} dx$

5. $\int \frac{2x^5 - 2x^4 + 4}{x^4 - 4x^2} dx$

6. $\int \frac{x^2 + 2x + 4}{x^4 - 5x^2 + 4} dx$

7. $\int \frac{\cos^5 x dx}{\sin^3 x}$

8. $\int \frac{\sin x + \cos x}{3 + \sin 2x} dx$

9. $\int \frac{1}{(x+1)^2} \sqrt{\frac{1-x}{1+x}} dx$

10. $\int \frac{5x dx}{\sqrt{1+x^4}}$

Вариант 17

1. $\int \frac{(1 - \cos 2x) dx}{6 \sin x}$

2. $\int \frac{\sqrt{4 - e^{-x}} x}{e^x} dx$

3. $\int \frac{5x - 2}{\sqrt{-6x + x^2}} dx$

4. $\int x \ln \frac{1+x}{1-x} dx$

5. $\int \frac{3x^3 + 1}{x^2 - 1} dx$

6. $\int \frac{x^3 + 4x^2 + 4x + 2}{(x+1)^2(x^2 + x + 1)} dx$

7. $\int \frac{dx}{\sqrt{\sin x \cos^3 x}}$

8. $\int \frac{(1 + \operatorname{ctg} x) dx}{1 - \operatorname{cgt} x}$

9. $\int \frac{5x + \sqrt{4x + 4}}{\sqrt[3]{8x + 8}} dx$

10. $\int \frac{dx}{x^4 \sqrt{x^2 - 1}}$

Вариант 18.

1. $\int \frac{\sin 3x - \sin 5x}{\cos 4x} dx$

2. $\int \frac{\ln x dx}{x\sqrt{1 - \ln x}}$

3. $\int \frac{3x - 1}{\sqrt{4 - 6x + 2x^2}} dx$

4. $\int \frac{\operatorname{arctg} e^x}{e^x} dx$

5. $\int \frac{-x^5 + 9x^3 + 4}{x^2 + 3x} dx$

6. $\int \frac{x}{x^4 - 4x^2 + 3} dx$

7. $\int \frac{\sin^3 x dx}{\sqrt{\cos x}}$

8. $\int \frac{\cos^3 x dx}{4\sin^2 x - 1}$

9. $\int \frac{dx}{\sqrt{x+3} + \sqrt[3]{x+3}}$

10. $\int \frac{dx}{x\sqrt{x^2 + x + 1}}$

Вариант 19.

1. $\int \frac{\operatorname{tg} \frac{x}{2}}{1 - \operatorname{tg}^2 \frac{x}{2}} dx$

2. $\int \frac{2^{\operatorname{arctg} x} + 2x^2}{1 + x^2} dx$

3. $\int \frac{2x - 3}{\sqrt{1 - x - x^2}} dx$

4. $\int x \arcsin \frac{1}{x} dx$

5. $\int \frac{2x^2 + 4}{(x - 4)(x + 2)} dx$

6. $\int \frac{5x - 13}{(x^2 - 5x + 6)^2} dx$

7. $\int \operatorname{ctg}^3 3x dx$

8. $\int \frac{dx}{\sin^2 x - 5 \cos x \sin x}$

9. $\int \sqrt{\frac{2 - x}{x - 6}} dx$

10. $\int x \sqrt{x^2 + 2x + 2} dx$

Вариант 20.

1. $\int \frac{\cos^2 x}{1 - \sin x} dx$

2. $\int x^2 \operatorname{ctg}^2(x^3 - 3) dx$

3. $\int \frac{3x + 2}{\sqrt{1 - x - 2x^2}} dx$

4. $\int \frac{\ln(\sin x)}{\sin^2 x} dx$

5. $\int \frac{x^3}{(x-1)(x+1)(x+2)} dx$

6. $\int \frac{x^3 + 6x^2 + 13x + 9}{(x+1)(x+2)^2} dx$

7. $\int \sin 6x \cos^3 x dx$

8. $\int \frac{\sin 2x dx}{-\sin^2 x + \cos^3 x - 1}$

9. $\int \frac{dx}{(2-x)\sqrt{1-x}}$

10. $\int \frac{dx}{(1-x^2)\sqrt{1-x^4}}$