

1	$\int dx = x$	$\int x dx = \frac{x^2}{2}$	13	$\int \frac{dx}{1+x^2} = \text{arctg}x$	$\int \frac{dx}{a^2+x^2} = \frac{1}{a} \text{arctg} \frac{x}{a}$
2	$\int \frac{dx}{x^2} = -\frac{1}{x}$	$\int \frac{dx}{\sqrt{x}} = 2\sqrt{x}$	14	$\int \frac{dx}{x^2-1} = \frac{1}{2} \ln \left \frac{x-1}{x+1} \right $	$\int \frac{dx}{x^2-a^2} = \frac{1}{2a} \ln \left \frac{x-a}{x+a} \right $
3	$\int x^\alpha dx = \frac{x^{\alpha+1}}{\alpha+1}; \quad \underline{\alpha \neq -1}$		15	$\int \frac{dx}{\sqrt{x^2 \pm k}} = \ln \left x + \sqrt{x^2 \pm k} \right $	
4	$\int \frac{dx}{x} = \ln x $	$\int \frac{dx}{\alpha x + \beta} = \frac{1}{\alpha} \ln \alpha x + \beta $	16	$\int \frac{dx}{\sqrt{1-x^2}} = \arcsin x = -\arccos x$	$\int \frac{dx}{\sqrt{a^2-x^2}} = \arcsin \frac{x}{a} = -\arccos \frac{x}{a}$
5	$\int e^x dx = e^x$	$\int e^{\alpha x} dx = \frac{1}{\alpha} e^{\alpha x}$	17	$\int \sqrt{x^2+k} dx = \frac{x\sqrt{x^2+k}}{2} + \frac{k}{2} \ln x+\sqrt{x^2+k} $	
6	$\int a^x dx = \frac{a^x}{\ln a}$	$\int a^{\lambda x} dx = \frac{1}{\lambda \ln a} a^{\lambda x}$	18	$\int \sqrt{a^2-x^2} dx = \frac{x\sqrt{a^2-x^2}}{2} + \frac{a^2}{2} \arcsin \frac{x}{a}$	
7	$\int \sin x dx = -\cos x$	$\int \sin \alpha x dx = -\frac{1}{\alpha} \cos \alpha x$	19	$\int \text{sh}x dx = \text{ch}x$	
8	$\int \cos x dx = \sin x$	$\int \cos \alpha x dx = \frac{1}{\alpha} \sin \alpha x$	20	$\int \text{ch}x dx = \text{sh}x$	
9	$\int \text{tg}x dx = -\ln \cos x $	$\int \text{tg} \alpha x dx = -\frac{1}{\alpha} \ln \cos \alpha x $	21	$\int \frac{1}{\text{sh}^2 x} dx = -\text{cth}x$	
10	$\int \text{ctg}x dx = \ln \sin x $	$\int \text{ctg} \alpha x dx = \frac{1}{\alpha} \ln \sin \alpha x $	22	$\int \frac{1}{\text{ch}^2 x} dx = \text{th}x$	
11	$\int \frac{dx}{\cos^2 x} = \text{tg}x$	$\int \frac{dx}{\cos^2 \alpha x} = \frac{1}{\alpha} \text{tg} \alpha x$	23	$\int \frac{dx}{\cos x} = \frac{1}{2} \ln \left \frac{\sin x + 1}{\sin x - 1} \right $	
12	$\int \frac{dx}{\sin^2 x} = -\text{ctg}x$	$\int \frac{dx}{\sin^2 \alpha x} = -\frac{1}{\alpha} \text{ctg} \alpha x$	24	$\int \frac{dx}{\sin x} = \frac{1}{2} \ln \left \frac{\cos x - 1}{\cos x + 1} \right $	
	$\sin(2x)dx = d(\sin^2 x) = -d(\cos^2 x)$			$t = \sin^2 x; \quad dt = \sin(2x)dx$	
				$t = \cos^2 x; \quad dt = -\sin(2x)dx$	

Свойства интегралов: $\int (C_1 f(x) + C_2 g(x)) dx = C_1 \int f(x) dx + C_2 \int g(x) dx$

Замена переменных $\int f(\varphi(x)) \cdot \varphi'(x) dx = \int f(t) dt$; где $t = \varphi(x)$; $dt = \varphi'(x) dx$

в частности: $t = \alpha x + \beta$; $dt = \alpha dx$; $\int f(\alpha x + \beta) dx = \frac{1}{\alpha} F(\alpha x + \beta)$

Формула Ньютона-Лейбница $\int_a^b f(x) dx = F(x) \Big|_a^b = F(b) - F(a)$

Формула интегрирования по частям $\int u dv = u \cdot v - \int v du$